#### Introduction to Statistical Genetics and Genomics

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#### Outline

- Part I
  - Definitions & background
  - Statistical methods
- Part II
  - More advanced statistical modeling
  - Network Analysis
  - An example

# Part I Genetics and Statistics

# What is statistical genetics ?

- Statistical methods to analyze and make inferences from genetic data.
  - Discover genetic variants associated with traits or diseases



• DNA: deoxyribonucleic acid, the hereditary material in organisms



- Genome: organism's complete set of DNA
  - Human genome: 22 autosomal + sex chromosomes



• SNP: single nucleotide polymorphisms, the most common type of genetic variation among people.



• Linkage Disequilibrium: non-random association of alleles at different loci



• Association analysis: statistical method to identify disease susceptibility variants that contribute to a specific disease or phenotype.



• Linkage analysis: statistical method for mapping the genes for heritable traits to their chromosome locations



• Segregation analysis: statistical technique that attempts to explain the causes of family aggregation of disease



### **Association Analysis**

- Based on unrelated study subjects
- Aims to find an association between a disease trait and genetic marker
- Study designs:
  - Case-control
  - Cohort

**Statistical Methods for Association Analysis** 

Case-control study:

- Z/Chi-squared/Fisher test
- Logistic regression

#### **Statistical Methods for Association Analysis**

Case-control study:





#### GWAS Catalog https://www.ebi.ac.uk/gwas/diagram



#### GWAS Diagram Browser Exploring Genome-wide Association Studies

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Nucleic Acids Research https://doi.org/10.1093/nar/gkt1229

#### Population Stratification/Admixture

- Allele frequencies can differ substantially between different subpopulations
- Risk of disease can also differ substantially
- Inflates the number of false positive findings if not accounted for

# Multiple Testing

- GWAS tests many markers for genetic association
- For a single marker:
- $\alpha' = P(\text{reject null hypothesis } H^{(m)} | H^{(m)} \text{ is true})$
- For multiple markers:

 $\alpha = 1 - P(\text{not reject any } H^{(m)} | H^{(m)} \text{ is true for all } m)$ =  $1 - (1 - \alpha')^M = 1$ 

# Multiple Testing

- Bonferroni correction method:  $\alpha/M$
- Threshold of  $5 \times 10^{-8}$

#### Some more statistics...

# Simple Linear Regression

Goals:

\*To identify the form of the functional relationship between two variables X and Y
\*To construct a mathematical model that best fits the data



# X: the independent variable or the predictorY: the dependent variable or the response

# **Model Assumptions**

- •The independent variable X is fixed, i.e. its values are predetermined or chosen in advance
- •The independent variable X is measured without error

This generates a FIXED EFFECT model

# **Model Assumptions**

For each value of X there exists a sub-population of Y values with the following characteristics

Linearity Independency Normality Equal Variance



The means of the sub-populations Y all lie on the same straight line

$$\mu_{Y|X} = \beta_0 + \beta_1 X$$

 $m_{Y|X}$  is the mean of the subpopulation Y given a particular value of X



- •The Y values are statistically independent
- •The subpopulations of Y given X are independent



# •The subpopulations of Y|X are all normally distributed

### Equal Variance

# •The subpopulations of Y|X all have the same variance s<sup>2</sup>

# **Regression Equation**

All regression assumptions can be summarized by the regression equation

$$y_i = \beta_0 + \beta_1 X_i + e_i$$

where

$$e_i \sim N(0, \sigma^2)$$

It follows that

 $y_i \sim N(\beta_0 + \beta_1 X_i, \sigma^2)$ 

#### Model

#### Theoretical model:



#### Model

#### Estimated model:



# Interpretation

- $\hat{y}$  is the value of the dependent variable that we predict from the model
- $\beta_0$  Is the predicted value of the dependent variable for X=0
- $\hat{\beta}_1$  Indicates the rate of change in Y for each

unit increment of X The sign of  $\hat{\beta}_1$  indicates the direction of the change

The magnitude of  $\hat{\beta}_1$  indicates the speed of change

### Multiple Linear Regression

•Multiple regression is an extension of the simple regression model where more than one predictors are considered.

- Example:
- Simple linear model: SBP is a function of sodium intake
- Multiple regression: SBP is a function of sodium intake, age, exercise, etc.

### Multiple Linear Regression

- •To improve the predicting ability of the model
- •To test interactions among predictors
- •To correct for the effect of confounders
- •To improve goodness of fit

# Multiple Linear Regression

- 1.More difficult to choose more candidate predictors are available
- 2.More difficult to visualize multidimensional space
- 3.More difficult to interpret many predictors
- 4.More difficult notation matrix notation needed for calculations
- 5.Computations: cannot do by hand need computer
## Multiple Linear Regression

$$Y = \beta_0 + \beta_1 X_1 + \beta_2 X_2 + \dots + \beta_p X_p + e$$

where  $\beta_0, \beta_1, \beta_2, ..., \beta_p$  are the regression coefficients,

and  $X_1, X_2, ..., X_p$  are the predictors

## Multiple Linear Regression

$$y_{i} = \beta_{0} + \beta_{1}x_{i1} + \beta_{2}x_{i2} + e_{i}$$

Model with two predictors The model defines a plane in a three dimensional space  $(Y, X_1, X_2)$ 



# Multiple Linear Regression

EXAMPLE: Y = SBP,  $X_1$  = sodium intake,  $X_2$  = Age

$$\hat{Y} = \hat{\beta}_0 + \hat{\beta}_1 X_1 + \hat{\beta}_2 X_2$$

 $\hat{\beta}_0$  Is the value of SBP when BOTH sodium intake and age are =0

 $\beta_1$  Is the change in SBP for each unit change in sodium intake when age IS HELD CONSTANT

 $\hat{\beta}_2$  Is the change in SBP for each unit change in age when sodium intake IS HELD CONSTANT

# **Model Assumptions**

As for the simple linear model 1.Linearity 2.Independency 3.Normality 4.Equal variance

# Logistic Regression

- Outcome is discrete, not continuous
- Involves a more probabilistic view of classification it into a real number z in the range  $\infty$  to +  $\infty$

$$z = \alpha + \mathbf{\beta} \cdot \mathbf{x} = \alpha + \beta_1 x_1 + \dots + \beta_d x_d$$

$$z = \log\left(\frac{p \neq 1}{1-p}\right) (1+e_{\text{log}}) \text{ function}$$

$$p = z$$

# Regularization

- Shrink the coefficients in the resulting model to avoid overfit by penalizing certain values of the weights
- Helps the computational problem
- Helps with generalization



Part II Genomics and Network Analysis

## Introduction to Statistical Genetics and Genomics

Umut Özbek, PhD Associate Professor of Biostatistics Tisch Cancer Institute Department of Population Health Science & Policy Part II Genomics and Network Analysis

## Network Analysis

Network analysis in biology

Biological systems are often represented as networks which are complex sets of binary interactions between entities.



# **Graph Theory**



Set of abstract concepts that can be used to visualize and analyze networks.
Made up of nodes which are connected by edges.

•Topology is the way in which the nodes and edges are arranged within a network.

Some history...

•The idea of topology first described by the Swiss mathematician Leonhard Euler: Seven bridges of Königsberg

### Seven bridges of Königsberg

Four islands connected by seven bridges



Is there a path that visited all four islands and crossed each of the bridges only once?

### Seven bridges of Königsberg Euler: -only the relations between the land masses are relevant. -land masses are the nodes. -bridges are the edges. -the path does not exist.



Network topology

Topological properties:

Shortest path: shortest distance between any two node.



### Network topology

Topological properties:

- Degree: number of edges that connect to a node.



### Network topology



Topological properties:

- Topological clusters: groups of nodes that are more internally connected than they are with the rest of the network.

### Types of network edges



### Adjacency matrices



# The Cancer Genome Atlas (TCGA) Research Network NCI/NHGRI

- Comprehensive genomic data to understand the molecular basis of cancer
- 33 cancer types
- Tumor and matched normal tissues from 11,000 patients
- Publicly available

#### **The Cancer Genome Atlas Research Network**



Courtesy of Dr. Boris Reva

Achievements of TCGA

- Large scale view on genomic landscapes in cancer
  - Major driver genes
  - Major altered cancer pathways
- Insights into complexity and inherent diversity of cancer
- Understanding necessity of personalized approach to treat cancer

### Giant piles of TCGA data



"Clinical researchers use the Atlas to match patient molecular profiles to a specific tumor subtype.

Biotech companies use the Atlas to extract potential drug targets and new indications.

Progress in DNA sequencing, IT, and analytical technologies adds more detail to the Atlas, **and lower prices make genomic characterization available to more patients**."

Linda Chin, TCGA pioneer

#### **Targeted therapy for cancer**

"**Targeted therapies** are drugs that interfere with a specific biochemical pathway that is central to the development, growth and spread of that particular cancer."

Then, a general **computational task** for targeted cancer therapy:

Given a molecular profile of a tumor and a set of molecular profiles of tumors with characterized driving alterations, determine

- activated cancer genes, gene modules and pathways
- targets for therapeutic interventions
- targets for known drug

Setting "targeted therapy" as a computational problem implies application of powerful approaches developed in data analysis, network modeling, pattern recognition and machine learning....

#### Targeted therapy as a "target finding" problem



## **Integrative Analysis**

• Integrating multiple molecular information leads to higher level discoveries of cell biology

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- Models that integrate omic data types rather than one model per type

- Integrating multiple molecular information leads to higher level discoveries of cell biology
- Models that integrate omic data types rather than one model per type
- Model scope: N << P

### • Using only a subset of all possible interactions

- Using only a subset of all possible interactions
- Data types cannot be modeled by Normal distributions

**Sparse Conditional Gaussian Graphical Model (SCGGM), Zhang and Kim, 2014** 

- Conditional Gaussian graphical model
- Fits models through an *l*<sub>1</sub> penalized conditional log-likelihood

## SCGGM

$$(Y_i, X_i) \sim_{i.i.d.} \mathcal{N}(0, \Sigma), i = 1, \dots, N$$
  
joint covariance:  $\Sigma = \begin{pmatrix} \Sigma_{xx} & \Sigma_{xy} \\ \Sigma_{yx} & \Sigma_{yy} \end{pmatrix}$   
concentration matrix:  $\Sigma^{-1} = \begin{pmatrix} \Theta_{xx} & \Theta_{xy} \\ \Theta_{yx} & \Theta_{yy} \end{pmatrix}$   
The conditional p.d.f for the CGM is:

$$Y_i|X_i \sim N(-\Theta_{yy}^{-1}\Theta_{yx}X_i,\Theta_{yy}^{-1})$$

Like the GGM, the goal is to learn the zero (and non-zero) entries of  $\Theta_{xy}, \Theta_{yy}$ .

### **spaceMap** Conley et al. 2018

- Conditional graphical model
- Learns the conditional dependencies between two types of nodes through a penalized multivariate regression framework
- Cross-validation and model aggregation for reproducibility

## spaceMap

For j = 1, ..., Q: regress  $Y_j$  on predictors  $\{Y_{-(j)}, X_l : l = 1, ..., P\}$ 

$$Y_j = \sum_{j \neq k} \rho^{jk} \sqrt{\sigma_{kk} / \sigma_{jj}} Y_k + \sum_{l=1}^P \gamma_{jl} X_l + \epsilon_j$$

Minimize penalized least-squares criterion:

$$L_{N,\lambda}(\theta, \sigma, \Gamma) = \frac{1}{2} \sum_{j=1}^{Q} \left( Y_{j} - \sum_{j \neq k} \rho^{jk} \sqrt{\sigma_{kk} / \sigma_{jj}} Y_{k} - \sum_{l=1}^{P} \gamma_{jl} X_{l} \right)^{2} + \lambda_{1} \sum_{1 \leq j < k \leq Q} |\rho^{jk}| + \lambda_{2} \sum_{l=1}^{P} ||\Gamma_{l}||_{1} + \lambda_{3} \sum_{l=1}^{P} ||\Gamma_{l}||_{2}$$

The  $\beta_{jk}$ 's &  $\gamma_{jl}$ 's are proportional to the partial correlations  $Cor(y_j, y_k | y_{-(j,k)}, x)$  &  $Cor(y_j, x_l | y_{-(j)}, x_{-(l)})$ , respectively.



# Hypothesis

Genes that are driven by CNAs would affect the protein activities and should be more informative for ovarian cancer survival.


#### **Cell-cycle and RTK pathways**



### **The Pan-Cancer Atlas**

- Extension of TCGA
- Completed in 2018
- Alterations across different tumor types

https://www.cell.com/pb-assets/consortium/PanCancerAtlas/PanCani3/index.html



**Oncogenic Processes** 

# Cell of Origin Patterns

**Cell-of-Origin Patterns Dominate the Molecular Classification of 10,000 Tumors from 33 Types of Cancer** 

- Machine Learning Identifies Stemness Features Associated with Oncogenic Dedifferentiation
- A Comprehensive Pan-Cancer Molecular Study of Gynecologic and Breast Cancers

• Comparative Molecular Analysis of Gastrointestinal Adenocarcinomas

### Cell-of-Origin Patterns Dominate the Molecular Classification of 10,000 Tumors from 33 Types of Cancer (2018)



http://www.cell.com/cell/fulltext/S0092-8674(18)30302-7?utm\_campaign=STMJ\_1522958526\_SC&utm\_channel=WEB&utm\_source=WEB&dgcid=STMJ\_1522958526\_SC

#### Cell-of-Origin Patterns Dominate the Molecular Classification of 10,000 Tumors from 33 Types of Cancer (2018)

iCluster:

- Joint latent variable model for integrative clustering.
- Incorporates flexible modeling of the associations between different data types and the variance-covariance structure within data types in a single framework, while simultaneously reducing the dimensionality of the datasets.
- Likelihood-based inference is obtained through the Expectation-Maximization algorithm.

Cluster-of-cluster assignments (COCA):

- Takes as input the binary vectors that represent each of the platform-specific cluster groups.
- Reclusters the samples according to those vectors.
- Data across platforms are combined without the need for normalization.
- Each platform influences the final integrated result with weight proportional to the number of distinct subtypes reproducibly found by consensus clustering.



## Conclusions

- Identified 10 to 25 platform-specific molecular subsets within ~10,000 tumors, each showing significant compositional heterogeneity based on classical tumor taxonomy.
- These iCluster assignments have potential clinical utility, and their multi-platform basis suggests that this new subclassification system might further improve the management of the 1%–3% of all cancer patients newly diagnosed with cancer of unknown primary (CUP).
- Interrogation of individual iClusters for their differentiating PARADIGM pathway features, canonical pathways, and gene programs amenable to drug targeting identified strong immune-related signaling features, suggesting that they may share potential susceptibility to immunotherapy.
- Integrated molecular tumor profiling may improve basket-trial design by considering both mutations and oncogenic signaling pathways along with consideration of each tumor's tissue-specific or cell-of-origin context.

# **Oncogenic Processes**

## **Perspective on Oncogenic Processes at the End of the Beginning of Cancer Genomics**

- Pathogenic Germline Variants in 10,389 Adult Cancers
- Comprehensive Characterization of Cancer Driver Genes and Mutations
- Driver Fusions and Their Implications in the Development and Treatment of Human Cancers

### Perspective on Oncogenic Processes at the End of the Beginning of Cancer Genomics (2018)

#### THE CANCER GENOME ATLAS



http://www.cell.com/cell/fulltext/ S0092-8674(18)30313-1? utm\_campaign=STMJ\_1522958526\_SC&utm \_channel=WEB&utm\_source=WEB&dgcid=S TMJ\_1522958526\_SC

#### Perspective on Oncogenic Processes at the End of the Beginning of Cancer Genomics (2018)



## Conclusions

- The germline genome has far-ranging, pathway-dependent influences on the somatic landscape, often promoting somatic mutations.
- Interactions between driver genes and the transcriptome are context dependent, as is the impact of driver mutations in both *cis* and *trans*-expression.
- Some oncogenic processes that tend to be deregulated in few cancer types are more related to specific genes rather than to prominent drivers.
- Findings suggest drastic changes in clinical practice and drug development:
  - Molecular treatments will increasingly be developed with multi-omics.
  - Bioinformatic systems will help efficiently design optimized treatment plans lurking within large combinatorial spaces with respect to dosage, efficacy, side effects, etc.

Could some somatic mutations be tolerated in normal development? How does this impact our understanding of oncogenic mutations? Can we find the alterations that drive the process from primary tumor to metastases?

# Signaling Pathways

**Oncogenic Signaling Pathways in The Cancer Genome Atlas** 

- Pan-cancer Alterations of the MYC Oncogene and Its Proximal Network across the Cancer Genome Atlas
- Machine Learning Detects Pan-cancer Ras Pathway Activation in The Cancer Genome Atlas
- Genomic and Molecular Landscape of DNA Damage Repair Deficiency across The Cancer Genome Atlas

### **Oncogenic Signaling Pathways in The Cancer Genome Atlas (2018)**



http://www.cell.com/cell/fulltext/ S0092-8674(18)30359-3? utm\_campaign=STMJ\_1522958526\_SC&utm\_cha nnel=WEB&utm\_source=WEB&dgcid=STMJ\_152 2958526\_SC



utm\_campaign=STMJ\_1522958526\_SC&utm\_channel=WEB&utm\_source=WEB&dgcid=STMJ\_15229 58526 SC

## Conclusions

- Signaling pathways are somatically altered in cancer at varying frequencies and in varying combinations across different organs and tissues.
- There is a complex interplay of co-occurring and mutually exclusive alterations within and across pathways.
- Standardized set of pathway templates, curated through a combination of computational methods and expert review are reported and publicly available (<u>http://pathwaymapper.org/</u>).
- Most hematologic cancers are not included.



- How can we improve medicine with genetics and genomics research?
- Is it possible to implement the findings?

### **Basket Trials**

- Basket trials are prospective clinical trials that test one or more targeted interventions across multiple types of diseases.
- There are unifying eligibility criteria usually based on a patient's predictive risk factor.

### **Basket Trials**



Control

https://acsjournals.onlinelibrary.wiley.com/doi/epdf/10.3322/caac.21600

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intervention

## **Umbrella** Trials

- Umbrella trials are prospective clinical trials that test multiple targeted interventions for a single disease based on predictive biomarkers or other predictive patient risk factors.
- In umbrella trials, a single disease (eg, advanced breast cancer) is stratified into multiple subgroups, with eligibility for each intervention arm defined by the intervention's mechanism of action.

### **Umbrella** Trials



B Umbrella trial - with controls



https://acsjournals.onlinelibrary.wiley.com/doi/epdf/10.3322/caac.21600

### **Basket and Umbrella Trials**

| KEY CHARACTERISTICS       | BASKET TRIALS                                                                                                                                                        | UMBRELLA TRIALS                                                                                                                                                                           |
|---------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Eligibility criteria      | <ul> <li>Patients enrolled in a basket trial have multiple diseases with<br/>common unifying risk factor(s)</li> </ul>                                               | • Patients in an umbrella trial usually have the same disease                                                                                                                             |
| Patient subgroups         | <ul> <li>Patient subgroups may be defined based on disease subtypes</li> </ul>                                                                                       | <ul> <li>Risk factors are used to stratify patients into multiple<br/>subgroups (<i>patient stratification</i>)</li> </ul>                                                                |
| Intervention assignment   | <ul> <li>It is common for basket trials to have a single intervention<br/>that is targeted based on the unifying risk factor</li> </ul>                              | <ul> <li>Umbrella trials have multiple interventions, with intervention<br/>assignment being determined based on their risk factor</li> </ul>                                             |
|                           | <ul> <li>Intervention assignment may or may not be determined using randomization</li> </ul>                                                                         | <ul> <li>Similar to basket trials, intervention assignment may or may<br/>not be determined using randomization</li> </ul>                                                                |
| Choice in a control group | <ul> <li>Determining the choice in the control group can be<br/>difficult because there are multiple diseases being<br/>studied</li> </ul>                           | • Compared with basket trials, it may be easier to pick the choice in the control group for umbrella trials because there is one disease being studied                                    |
|                           | <ul> <li>If there are different established standards of care between<br/>multiple diseases being studied, a common control group may<br/>not be feasible</li> </ul> | <ul> <li>The existing standard of care (or placebo, if there is no<br/>established care) for the disease being studied may be used<br/>as the control for all of the subgroups</li> </ul> |
|                           |                                                                                                                                                                      |                                                                                                                                                                                           |

THANK YOU!